

Paths characteristics in determination of optimal clustering procedure for a data set

No.	Steps in a typical cluster analysis	Path's number									
		1	2	3	4	5	6	7	8	9	
I	Selection of objects and variables	data matrix $[x_{ij}]$									
II	Measurement scale of variables	ratio	ratio	interval or mixed ¹	ordinal ²	multi-state nominal ³	binary	ratio	interval or mixed ¹	ratio	interval or mixed ¹
	Selection of normalization formula ⁴	$n6 - n11$	$n1 - n5$	$n1 - n5$	N.A.	N.A.		without normalization		$n6-n11 / n1-n5$	$n1-n5$
	Transformed measurement scale of variables	ratio	interval	interval	ordinal	multi-state nominal	binary	ratio	interval or mixed ¹	ratio / interval	interval
III	Selection of distance measure ⁵	$d1 - d7$	$d1 - d5$	$d1 - d5$	$d8$	$d9$	$b1 - b10$	$d1 - d7$	$d1 - d5$	N.A.	
IV	Selection of clustering method ⁶	$m1 - m8$								$m9$	
V	Maximal number of possible variants	$[(6 \times 7 \times 5) + (6 \times 1 \times 3)] + [(5 \times 5 \times 5) + (5 \times 1 \times 3)] = 368$		$(5 \times 5 \times 5) + (5 \times 1 \times 3) = 140$	$1 \times 5 = 5$	$1 \times 5 = 5$	$10 \times 5 = 50$	$(7 \times 5) + (1 \times 3) = 38$	$(5 \times 5) + (1 \times 3) = 28$	11	5
	Number of all classifications	$LK = (\maxClusterNo - \minClusterNo + 1) \cdot LW_p$, where \minClusterNo – minimal number of clusters, \maxClusterNo – maximal number of clusters, LW_p – number of variants for p -th path.									
	Internal cluster quality index	1. Calinski & Harabasz (G1) ⁷ 2. Baker & Hubert (G2) 3. Hubert & Levin (G3) 4. Silhouette (S) 5. Krzanowski & Lai (KL) ⁷				1. N.A. 2. G2 3. G3 4. S 5. N.A.		1. G1 2. G2 3. G3 4. S 5. KL		1. G1 2. N.A. 3. N.A. 4. N.A. 5. KL	

¹ Ratio & interval.² We can use ratio, interval or mixed data (ratio, interval, ordinal), however these data are treated as ordinal because in the construction of the GDM2 distance measure only such relations as: "equal to", "higher than", "lower than" are taken into account.³ We can use ratio, interval, ordinal or mixed data (ratio, interval, ordinal, nominal), however these data are treated as nominal because in the construction of the Sokal & Michener distance measure only such relations as: "equal to", "not equal to" are taken into account.⁴ $n1 - (x-mean)/sd$, $n2 - (x-Me)/MAD$, $n3 - (x-mean)/range$, $n4 - (x-min)/range$, $n5 - (x-mean)/\max[abs(x-mean)]$, $n6 - (x/sd)$, $n7 - (x/range)$, $n8 - (x/\max)$, $n9 - (x/mean)$, $n10 - (x/sum)$, $n11 - x/\sqrt{SSQ}$.⁵ $d1 -$ Manhattan, $d2 -$ Euclidean, $d3 -$ Chebychev (max), $d4 -$ squared Euclidean, $d5 -$ GDM1, $d6 -$ Canberra, $d7 -$ Bray-Curtis; $d8 -$ GDM2, $d9 -$ Sokal & Michener; $b1 - b10$ (available in R `dist.binary` procedure): $b1 =$ Jaccard; $b2 =$ Sokal & Michener; $b3 =$ Sokal & Sneath (1); $b4 =$ Rogers & Tanimoto; $b5 =$ Czekanowski; $b6 =$ Gower & Legendre (1); $b7 =$ Ochiai; $b8 =$ Sokal & Sneath (2); $b9 =$ Phi of Pearson; $b10 =$ Gower & Legendre (2).⁶ $m1 -$ single link, $m2 -$ complete link, $m3 -$ average link, $m4 -$ McQuitty, $m5 -$ k -medoids (PAM), $m6 -$ ward, $m7 -$ centroid, $m8 -$ median, $m9 -$ k -means. For clustering methods $m6 - m8$ squared Euclidean distance is used only.⁷ with argument `centrotypes="centroids"`.

N.A. – Not Applicable.